

QUIZ 3

1. Evaluate the definite integrals:

(9)

(a)
$$\int_4^9 \left(\sqrt{x} + \frac{1}{2x} \right) dx =$$

(b)
$$\int_0^{\sqrt{2}} x e^{x^2} dx =$$

(c)
$$\int_1^2 \frac{2x+1}{(x^2+x)^3} dx =$$

2. Find the area between the curve $y = (2x+3)^2$ and the x -axis, from $x = -2$ to $x = 3$. (5)

3. Find the area between the curves $y = 4x - 3$ and $y = x^2$. (6)

4. Let $f(x)$ be a function, with antiderivative $F(x) = \int f(x) dx$ satisfying $F(1) = 2$, $F(3) = 4$. Compute: (6)

(a) $\int_1^3 f(x) dx =$

(b) $\int_0^6 f(x) dx + \int_6^0 f(x) dx =$

(c) $\int_1^3 2f(x) dx - \int_1^3 5f(x) dx =$

(d) $\int_1^2 f(x) dx + \int_2^3 f(x) dx =$

(e) $\int_3^3 \sqrt{f(x)} dx =$

5. Let $G(x) = \int_2^{x^2} \frac{1}{1 + \sqrt{t}} dt$. Find $G'(9)$. (4)

Table of Derivatives

$$\begin{array}{lll}
 (fg)' = f'g + fg' & \left(\frac{f}{g}\right)' = \frac{f'g - fg'}{g^2} & f(g(x))' = f'(g(x)) \cdot g'(x) \\
 (x^n)' = nx^{n-1} & (e^x)' = e^x & (\ln x)' = \frac{1}{x} \\
 (\sin x)' = \cos x & (\cos x)' = -\sin x & (\arctan x)' = \frac{1}{x^2 + 1}
 \end{array}$$

Table of Antiderivatives

$$\begin{array}{l}
 \int a \, dx = ax + C \\
 \int x^n \, dx = \frac{x^{n+1}}{n+1} + C \quad (n \neq -1) \\
 \int \frac{1}{x} \, dx = \ln |x| + C \\
 \int e^{ax} \, dx = \frac{1}{a} e^{ax} + C \quad (a \neq 0) \\
 \int \sin(ax) \, dx = -\frac{1}{a} \cos(ax) + C \quad (a \neq 0) \\
 \int \cos(ax) \, dx = \frac{1}{a} \sin(ax) + C \quad (a \neq 0)
 \end{array}$$

Properties of Integrals

$$\begin{array}{l}
 \int (af(x) + bg(x)) \, dx = a \int f(x) \, dx + b \int g(x) \, dx \\
 \int f(g(x))g'(x) \, dx = F(g(x)) + C, \quad \text{where } F' = f \\
 \int_a^b f(x) \, dx + \int_b^c f(x) \, dx = \int_a^c f(x) \, dx \\
 \int_a^b f(t) \, dt = F(b) - F(a), \quad \text{where } F' = f \\
 \frac{d}{dx} \left(\int_a^x f(t) \, dt \right) = f(x)
 \end{array}$$