Unidirectional Excitation of Radiative-Loss-Free Surface Plasmon Polaritons in \( PT \)-Symmetric Systems

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We investigate the excitation and propagation of surface plasmon polaritons (SPPs) at a geometrically flat metal-dielectric interface with a parity-time (\( PT \)) symmetric modulation on the permittivity \( \epsilon(x) \) of the dielectric medium. We show that two striking effects can be simultaneously achieved thanks to the nonreciprocal nature of the Bloch modes in the system. First, SPPs can be unidirectionally excited when light is normally incident on the interface. Secondly, the backscattering of SPPs into the far field is suppressed, producing a radiative-loss-free effect on the unidirectional SPPs. As a result, the lifetime and propagation distance of SPPs can be significantly improved. These results show that \( PT \) symmetry can be employed as a new approach to designing transformative nanoscale optical devices, such as low-loss plasmonic routers and isolators for efficient optical computation, communication, and information processing.

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For a long time, absorption characterized by the imaginary component \( (\epsilon_i) \) of the dielectric constant \( (\epsilon = \epsilon_r + i\epsilon_i) \) was believed to play an undesirable role in optics, and should be mitigated and even eliminated. However, with the novel concepts of non-Hermitian Hamiltonian \(^5\) and parity-time (\( PT \)) symmetry \(^6\)–\(^20\), recently there has been increasing interest in manipulating the dynamics of optical waves via controlling the distribution of \( \epsilon_i \). Through engineering the spatial variation of gain \( (\epsilon_i < 0) \) and loss \( (\epsilon_i > 0) \), various attractive phenomena and important applications have been proposed and demonstrated. For example, Guo et al. \(^6\) reported loss-induced optical transparency in specially designed pseudo-Hermitian guiding potentials. Longhi \(^8\) and Chong et al. \(^9\) discussed the realization of a coherent perfect absorber as the time-reversed counterpart of a laser. Lin et al. \(^10\) and Feng et al. \(^11\) studied the unidirectional invisibility and reflectionless waveguide based on \( PT \) symmetry. The conservation relations and anisotropic transmission resonances in one-dimensional \( PT \)-symmetric photonic heterostructures were analyzed by Ge et al. \(^13\). In Ref. \(^14\), Fleury et al. introduced a new mechanism to realize negative refraction and planar focusing using a pair of \( PT \)-symmetric metasurfaces. Peng et al. \(^15\) showed how to turn losses into gain by steering the parameters of a system to the vicinity of an exceptional point (EP). \( PT \) symmetry in other metamaterials \(^16\)–\(^19\) and its nonlinear optical effects \(^20\) have also been studied by various groups.

Surface optical waves, such as surface plasmon polaritons (SPPs), have attracted much attention in the past decades because of their quasi-two-dimensional and subwavelength nature \(^21\),\(^22\). An efficient means to manipulate SPPs, including directional excitation and a longer propagation distance (or equivalently a longer lifetime), is always desired because it determines the figure of merit of SPP-related applications \(^23\)–\(^30\). In this Letter we show that by using a \( PT \)-symmetric modulation on the permittivity of the dielectric medium adjacent to a metal, we can realize unique features of SPPs at a geometrically flat dielectric-metal interface. We demonstrate that with a properly designed spatial distribution of \( \epsilon_r \) and \( \epsilon_i \) in the spirit of \( PT \) symmetry, a unidirectional excitation of SPPs can be achieved even under the condition of normal incidence. Furthermore, the \( PT \)-symmetric configuration breaks the reciprocal back-and-forth mutual coupling between the propagating wave and SPPs, and produces a radiative-loss-free effect on the unidirectionally generated SPPs with substantially improved lifetime. The underlying mechanism of these novel effects is closely related to an EP of the \( PT \)-symmetric modulation, which is not due to a square root singularity and is fundamentally different from previous work \(^2\),\(^4\),\(^31\). Such unidirectional and radiative-loss-free SPPs can be utilized for many potential applications.

Figure 1 shows a schematic of the proposed structure under investigation. A metal slab with a dielectric constant of \( \epsilon_m < 0 \) occupies the space below \( y = 0 \). Above the metal we introduce a dielectric layer of thickness \( d \). The dielectric layer supports a \( PT \)-symmetric distribution of \( \epsilon(x) \) in the form of \(^5\),\(^32\),\(^33\)

\[
\epsilon(x) = \epsilon_d + A(\cos \beta x + iV_0 \sin \beta x).
\]

Parameter \( \epsilon_d \) represents the background dielectric constant, and the modulation strength \( A \) is much smaller than \( \epsilon_d \). The real part of \( \epsilon(x) \) is symmetric with respect to \( x = 0 \), while the imaginary part is antisymmetrically distributed. The interface at \( y = 0 \) is geometrically smooth. When the \( PT \)-symmetric modulation is absent (i.e., \( A = 0 \),
the normally incident beam simply oscillates inside the layer and gets reflected. When $A$ is not 0, the periodic modulation of the permittivity, that is, $\Delta \varepsilon(x) = A|\cos(\beta x) + i V_0 \sin(\beta x)|$, could provide the required phase matching condition to excite SPPs. By using COMSOL Multiphysics we simulate the interaction of a normally incident beam with the structure. Dielectric constants considered in the simulation are $\varepsilon_m = -100 + 4i$ [34] and $\varepsilon_d = 6$. The thickness $d$ of the dielectric layer is 0.29$\lambda_0$, and the beam width of incidence is 5$\lambda_0$, where $\lambda_0$ is the wavelength in vacuum. Parameter $\beta$ equals the real part of the wave vector of the corresponding SPP mode,

$$\beta = k_0 \sqrt{\frac{e_d \varepsilon_m}{e_d + e_m}},$$

where $k_0 = 2\pi/\lambda_0 = \omega_0/c$. Note that for a finite dielectric cladding layer the wave vector of SPPs may be different from Eq. (2), and an analytical formula can be found from [35]. However, Eq. (2) provides an accurate estimation of the necessary phase-matching wave vector when the permittivity modulation $\Delta \varepsilon(x)$ is small.

Figure 2(a) shows the transverse magnetic field component ($H_z$) when $V_0 = 0$. In this case, the dielectric constant $\varepsilon(x)$ is real everywhere, and a standard dielectric grating is realized. We can see that SPPs are equally excited on both sides of the incident beam, in agreement with the theory on the scattering of the optical wave by subwavelength gratings [21,22]. However, the characteristic of excited SPPs is distinctly different when $\mathcal{PT}$ symmetry is introduced into the dielectric layer. Figure 2(b) shows the result when $V_0 = 0.5$. We can see that by increasing the value of $V_0$, the excitation of SPPs along the forward and backward directions becomes unequal. SPPs are much more efficiently excited towards the left side of the incident beam. The degree of unequal SPP generation reaches its extreme scenario at the exceptional point of $V_0 = 1$, with which the excitation of SPPs on the right side of incidence is completely suppressed [see Fig. 2(c)]. Now a unidirectional excitation of SPPs is obtained. Note that the propagation direction of generated SPPs can be tuned by changing the sign of $V_0$, or to be more explicit, when $V_0 = -1$ SPPs are generated only on the right side of incidence.

The field distribution and its oscillation period agree well with the features of SPPs. From Figs. 2(d) and 2(e) we can see that the field is enhanced at the dielectric-metal interface, and the period of oscillation is given by $\beta \sim 2.526\lambda_0$, in very good agreement with Eq. (2). In addition to the asymmetric excitation of SPPs on opposite sides of incidence when $V_0$ increases, we also notice that the efficiency of SPP excitation is dependent on $V_0$. Figure 3 shows the distributions of the envelop of $H_z$ at the metal-dielectric interface for $V_0 = 0, 0.5,$ and 1, respectively. When $V_0 = 1$ the excitation of SPPs
Unidirectional excitation of SPPs has been previously demonstrated via controlling the polarization of illumination [25–27], or using asymmetric nanostructures [28–30]. These results can be well understood from the interference effect of SPPs. In contrast, the underlying mechanism of the unidirectional SPP generation and \( V_0 \)-dependent excitation efficiency in the \( PT \)-symmetric system is distinctly different, which can be explained by the nonreciprocal nature of the Bloch component through the Fourier analysis of \( \epsilon(x) \). Specifically, the periodical variation of the real and imaginary part of \( \epsilon(x) \) required by the \( PT \) symmetry can be expressed by using Fourier expansion. A simple expression of the modulation \( \Delta \epsilon(x) = A_c \cos(\beta x + i V_0 \sin(\beta x)) \) can be obtained as

\[
\Delta \epsilon(x) = A_L \exp(+i \beta x) + A_R \exp(-i \beta x),
\]

with

\[
A_L = A \frac{1 + V_0}{2},
\]

\[
A_R = A \frac{1 - V_0}{2}.
\]

Obviously, the factor \( \Delta \epsilon(x) \) contains two Bloch components \( \exp(-i \beta x) \) and \( \exp(+i \beta x) \) that represent moving harmonic gratings towards the forward and backward directions. When \( V_0 \) is not 0, \( A_L \) and \( A_R \) have different values, and the Fourier spectrum is nonreciprocal. On the other hand, the two wave vectors, \( +\beta \) and \( -\beta \), help to compensate the momentum mismatch between the normally incident wave (with \( k_z = 0 \)) and SPPs (with \( k_z = \pm \beta \)) according to Bloch’s theorem [21,22]. As a result, we expect to achieve asymmetric excitation of SPPs with the efficiency determined by \( A_L \) and \( A_R \), and ultimately by \( V_0 \).

The unique characteristics of SPPs in the \( PT \)-symmetric system can be analyzed by a simple perturbative approach and the coupled mode theory in a general context [36–38]. To include the damping effect, we can modify the Helmholtz equation for the magnetic field component \( H_z \) into the form of

\[
\nabla^2 H_z - \frac{\epsilon}{c^2} \left( \frac{\partial^2 H_z}{\partial t^2} + \frac{2}{\tau} (\partial H_z / \partial t) \right) = \Delta \epsilon / c^2 \left( \partial^2 H_z / \partial t^2 \right),
\]

where \( \tau \) represents the relaxation time. Specifically, \( \tau_{abs} \) is associated with the absorption loss of SPPs due to electron collision, and \( \tau_{rad} \) is related to the radiative loss. The mutual coupling among the three field components can be described by a non-Hermitian matrix over the complex amplitudes of SPPs (\( H_L^{SPP} \) and \( H_R^{SPP} \)) and free-space plane wave (\( H_Z \)) as follows

\[
\begin{bmatrix}
\omega_0 + i \tau_{abs} & A_L V^M & A_L V^N \\
A_R V^N & \omega_0 + i \tau_{rad} & A_R V^M \\
A_L V^M & A_R V^N & \omega_0 + i \tau_{abs}
\end{bmatrix}
\begin{bmatrix}
H_L^{SPP} \\
H_Z \\
H_R^{SPP}
\end{bmatrix}
= \hat{\omega}
\begin{bmatrix}
H_L^{SPP} \\
H_Z \\
H_R^{SPP}
\end{bmatrix}.
\]

If we use \( \Psi(y) \) to denote the field distribution of the excitation wave inside the \( PT \)-symmetric dielectric layer, and define \( \alpha = \sqrt{\beta^2 - \epsilon J_k^2} \), in Eq. (6) \( M = \left[ 1 - \exp(-2\alpha d) \right] / 2\alpha \) and \( N = \int_0^d \Psi(y)^* \Psi(y) dy \) are the field normalization factors of SPPs and the plane wave, respectively; \( V = -(\omega_0 / 2\epsilon) \int_0^d \Psi(y)^* e^{-\alpha y} dy \) characterizes the overlap integral of SPPs and the excitation wave obtained from a perturbative approach [36–38]. The detailed derivation of Eq. (6) can be found in Supplemental Material [39].

Being an analogue to a coupled three-level configuration in an atomic system [40,41], Eq. (6) usually leads to three complex solutions for frequency \( \hat{\omega} \) with modified dispersion and decay rate. However, it can be proved (see Supplemental Material [39]) that regardless of the complex solution \( \hat{\omega} \), the generated SPPs along the forward and backward directions have the identical ratio given by

\[
\frac{H_L^{SPP}}{H_R^{SPP}} = \frac{A_L}{A_R}.
\]

The weights of \( A_L \) and \( A_R \) determine the efficiency of SPP excitation. When \( V_0 = 0 \), the two harmonic contributions in \( \Delta \epsilon(x) \) have the identical weight of \( A/2 \) based on Eqs. (4) and (5). Therefore, the generated SPPs have equal amplitudes in the forward and backward directions [see Fig. 2(a)]. In contrast, \( A_L \) becomes greater than \( A_R \) when \( V_0 \) increases, and SPPs are more effectively generated on the left side of incidence.

The most interesting scenario takes place at the critical point of

\[
V_0 = 1, \quad A_R = 0.
\]

Albeit the excitation of SPPs on the right side of incidence is phase matched, the effective field \( A_R \) is 0. Now, because the eigensolutions coalesce [2–4,31] an atypical EP emerges, which is not due to a square root singularity.
i.e., the backward coupling of SPPs to free-space photons. This backward coupling process requires the harmonic term of $A_R \exp(-i\beta x)$. The efficiencies of these two opposite processes can be substantially different according to Eqs. (4) and (5). Equation (8) represents an extreme scenario of EP, in which

\[
\frac{1}{\tau_{\text{rad}}} = 0
\]

for the unidirectionally generated SPPs on the left side. This manifests that the backward scattering pathway is completely closed, resulting in the radiative-loss-free effect. Then the loss of SPPs, in theory, is only attributed to the absorption loss. The lifetime of the unidirectionally excited SPPs on the left side of incidence is expected to increase, producing long-range SPPs.

We conduct COMSOL simulations to confirm the predicted radiative-loss-free effect. The imaginary part of the permittivity of metal is set to be 0 (i.e., $\epsilon_m = -100$), in order to eliminate the absorption loss and help us to identify the role of backward scattering. Two cases are present here. The first case is similar to that in Fig. 2(c), with $A = 0.5$ and $V_0 = 1$, so that $A_L = 0.5$ and $A_R = 0$. The other case is that $A = 1$ and $V_0 = 0$, leading to $A_L = A_R = 0.5$. The only difference between these two cases is that the first one has a zero backward Bloch component $A_R$. From the results shown in Fig. 4(b) we indeed observe the radiative-loss-free effect in the first case. Both cases have equal initial magnitude of SPPs on the left side of incidence. However, when propagating away from the incident beam, SPPs in the first case of $V_0 = 1$ (red line) do not decay, while that of $V_0 = 0$ (blue line) shows an exponential decay, clearly indicating the presence of radiative loss. Furthermore, when $V_0 = 0$ the field possesses a weak oscillation. It is associated with the interference between SPPs and the cascading excited backward surface modes, and implies the existence of an open backward scattering pathway. Such a phenomenon does not arise when $V_0 = 1$.

Above demonstrated unidirectional radiative-loss-free SPP excitation shows great potential of $PT$ symmetry. Unidirectional SPP generation has been investigated via the utilization of vectorial near-field interference [25], interference among multiple elements on the metal surface [26–29], and compact coupled magnetic antennas [30]. Our approach is fundamentally different from previous work, because it relies not on the manipulation of localized scattering units, but on the global distribution of the refractive index in a geometric flat structure. Furthermore, losses in plasmonic structures and metamaterials have been noticed and are believed to be the main obstacle in impeding their practical applications [21–30,42–50]. One can engineer the shape of nanostructures to reduce the fraction of energy confined inside the metal and thus reduce the absorption loss [42–46], or introduce optical gain into the nanostructure to compensate the loss [47–50]. Our approach based on $PT$...
symmetry provides a new route to eliminate the radiative loss, which can be very strong when sharp edges, scattering, or microgratings are present. To the best of our knowledge, the mechanism of closing the backward scattering pathway by utilizing the nonreciprocal Bloch components in \(PT\)-symmetric systems has not been discussed before. Although we have focused on optical frequencies, the same strategy can be extended to microwave and THz regimes by using spoof SPPs on structured perfect conductors.\[51,52\]. It is worth pointing out that associated with the radiative-loss-free effect, the dispersion of SPPs is also immune to the \(PT\)-symmetric perturbation [see Eq. (10)]. This interesting characteristic may facilitate novel plasmonic designs.

In summary, we study the excitation of SPPs at a smooth metal-dielectric interface at normal incidence when the permittivity of the dielectric medium follows \(PT\) symmetry. It is shown that the loss and gain associated with the imaginary part of the dielectric constant can be engineered to realize unidirectional SPP excitation. We explain this novel effect by emphasizing that the \(PT\) symmetry produces different weights on the Bloch expansion terms with opposite wave vectors \(k = \pm \beta\). Such a unique property can also facilitate suppression and even eliminate the backward scattering from SPPs into free-propagating light waves, rendering a radiative-loss-free effect at an EP scenario. Full-wave simulations confirm our analytical predictions. Our results show that \(PT\) symmetry can find many potential applications in nanoscale optical devices, such as plasmonic routers and isolators for optical computation, communication, and information processing.

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[34] A comparable parameter can be obtained, for example, in silver around 1.3 \(\mu \text{m}\). See M. N. Polyanskiy, Refractive index database, http://refractiveindex.info.