The primacy of rhythm: how discrete actions merge into a stable rhythmic pattern

**Zhaoran Zhang**¹ and **Dagmar Sternad**²

¹Department of Bioengineering, Northeastern University, Boston, Massachusetts; and ²Department of Biology, Electrical and Computer Engineering, and Physics, Northeastern University, Boston, Massachusetts

Submitted 31 August 2018; accepted in final form 5 December 2018

**INTRODUCTION**

It is a well-known but intriguing observation that humans “fall into step” when walking side by side with a friend. When listening to music, one may inadvertently tap one’s foot to the beat, and when the audience applauds after a concert even a large collective of clapping hands can converge to a common rhythm (Strogatz 1994; Strogatz and Stewart 1993). More subtle synchronization occurs during social interactions when people unknowingly mimic each other’s rhythm in speech or body movements (Tolston et al. 2014). Such uni- and bidirectional synchronization between two or more oscillations is observed in a host of biological, physical, and social systems (Phillips-Silver et al. 2010; Strogatz 1994, 2004).

However, what happens if there is no external rhythm to synchronize with or if there is not even a rhythm at the outset? When humans repeat similar movements over a prolonged time, such as repetitive actions in the workplace, they sometimes experience themselves to be “in the flow,” a subjective state that can occur when a sequence of movements becomes increasingly more regular or periodic. Motivated by this anecdotal observation, the present study examined how people spontaneously fall into a rhythm when performing a series of discrete, goal-directed movements in the absence of any periodic cues. How does the repetition of similar movements performed at no specific intervals develop into a rhythmic pattern? Does this rhythmic pattern show features of dynamic stability, and if so, do such stable dynamics enable better performance? A brief caveat on terminology upfront: although “rhythm” in music and dance can be associated with a complex temporal pattern, we refer to rhythm as “approximately periodic” behavior, whereas strict “periodicity” is defined as a sequence of events separated by identical intervals. Furthermore, a rhythmic time series is continuous, in contrast to discrete movements that are separated by pauses (Hogan and Sternad 2007).

Rhythms are ubiquitous in the human body, including cortical, cardiac, respiratory, circadian rhythms, and tremor, both in functional and pathological expressions. These oscillations occur at many different temporal and spatial scales, comprising orders of magnitudes from $10^{-3}$ s in neural or informational processes to distributional processes operating at $10^6$ and $10^4$ and the metabolic system at $10^5$ s (Moser et al. 2006). These different mechanisms are coupled within and across spatiotemporal scales, likely to also manifest as rhythms at the behav-
ioral level. In return, behavioral rhythmicity may help to maintain the entrainment among the physiological processes of the body. For example, disturbances of the circadian rhythm lead to desynchronization between physiological rhythms, experienced as jetlag (Haus and Smolensky 2006). An extensive body of research has modeled these rhythms as nonlinear oscillators that, when coupled, can account for synchronized behavior in nature, ranging from circadian rhythms to the synchronous behavior of fireflies (Ermentrout and Kopell 1991; Kopell and Ermentrout 1986; Pikovsky et al. 2000; Rinzel and Ermentrout 1998; Strogatz 1994; Winfree 1967, 1990).

Recognition of the fundamental nature of rhythmicity in biological and physical systems is also the basis for a proposition in motor control: human movements rely on and exploit dynamic primitives; one such primitive is oscillations or rhythms (Hogan and Sternad 2012, 2013; Ijspeert et al. 2013; Ronssse et al. 2009; Schaal et al. 2000; Sternad 2008). Several previous lines of work have provided evidence that rhythmic movements are a basic form of organization that the neuromechanical system assembles and may use as building blocks in the control of voluntary movements. Importantly, these rhythmic patterns, or dynamic primitives, are presumed to have attractor properties, i.e., they have limit-cycle dynamics. Such stable oscillations arise at the neural level but may also comprise the neuromechanical system (de Rugy and Sternad 2003; Ronssse et al. 2009; Strogatz and Stewart 1993). The primary example has been legged locomotion that has been modeled as coupled oscillators (Full and Koditschek 1999; Ijspeert et al. 2013; Ochoa et al. 2017; Taga et al. 1991). However, biological movements are not only rhythmic but also display vastly more complex behaviors. Hence, several studies have suggested that other stable attractors exist, such as fixed points that are the basis for discrete point-to-point movements (Ijspeert et al. 2013; Ronssse et al. 2009; Sternad et al. 2000). Even chaotic attractors have been discussed as contributors to the observed variability (Raferty et al. 2008). Recent work has emphasized that, for interactions with objects, impedance is also needed as a dynamic operator (Hogan and Sternad 2012, 2013). If humans indeed fall into a stable rhythm when performing a series of actions, then this would provide strong support that rhythmic behavior is an attractor and a dynamic primitive for human behavior.

To investigate the spontaneous development of rhythmicity, we examined how human subjects practiced a virtual throwing task with the sole goal to hit a target. The instruction only emphasized that the target should be hit accurately, and rhythmic behavior is foundational for good task performance. This is consistent with the proposition that humans exploit dynamic primitives to not only simplify control, but also improve performance. When allowed to exploit stable attractor behavior, humans may free up attention for accuracy demands.

METHODS

Participants

Fifteen right-handed subjects (20.5 ± 2.8 yr; 7 women, 8 men) were recruited for experiment 1. All subjects were compensated with $55 after completing the 11 data collection sessions on 11 separate days. In experiment 2, 16 right-handed subjects (20.7 ± 2.8 yr; 9 women, 7 men) took part and were randomly assigned to one of two groups. Subjects received $30 after completing the six daily sessions of data collection. None of the subjects had any prior experience with the experimental task. All subjects signed the consent form of the protocol before the data collection; the study was approved by the Institutional Review Board at the Northeastern University.

Experimental Task and Apparatus

The experiments used a virtual throwing task that was based on the British pub game Skittles, which is similar to American tetherball (Fig. 1A) (Cohen and Sternad 2012; Hasson et al. 2016; Müller and Sternad 2004; Zhang et al. 2018). In this game, subjects throw a ball tethered to the top of a vertical post to hit a target skittle(s) on the opposite side of the post. For the virtual rendering, this task was presented as a top-down view on a backprojection screen (2 × 2 m) in front of the subject (distance to subject 1.50 m). The large red circle depicts the top-down view of the post; the smaller yellow circle represents the target to be hit (Fig. 1B). The purple bar corresponds to the subject’s arm/manipulandum and displayed his/her movements in real time. The white circle at the end of the bar is the ball to be thrown.

To perform the throwing movements, subjects rested their forearm on a manipulandum that restricted their movements to rotations in the horizontal plane (Fig. 1B). A wooden ball was fixed to the end of the manipulandum that had a force sensor attached to it (Interlink Electronics, Camarillo, CA). To initiate the throw, subjects grasped the ball and pressed their index finger on the force sensor to hold the virtual ball. To throw the ball, subjects moved their forearm and released the finger from the pressure sensor as in a Frisbee throw. Releasing the finger from the force sensor initiated the ball flight, and the ball trajectory was calculated from the online-measured angular position and velocity of the manipulandum at the release moment. After release, the ball traversed an elliptic trajectory around the post as shown in Fig. 1C. The top-down view simplified the physics of the task to a two-dimensional system in which the ball was suspended by two orthogonal, massless springs (Fig. 1C, inset). The equilibrium point of the ball was at the origin, which was defined at the center of variability at the Poincaré section. Finally, we assessed whether rhythmicity and stability in behavior correlated with task performance.

We hypothesized that the discrete throwing actions merge into a rhythmic sequence, identified by an approximately constant period and decreasing number and duration of pauses between movements (hypothesis 1). Subjects with higher degrees of rhythmicity and stability of their arm trajectories achieve better task performance (hypothesis 2). With increasing rhythmicity, the degree of stability of movements increases (hypothesis 3). When instructed to pause between successive throws, subjects perform worse than during self-paced rhythmic behavior (hypothesis 4). Results were indeed supportive of the hypotheses and allowed us to conclude that stable rhythmic behavior is foundational for good task performance. This is consistent with the proposition that humans exploit dynamic primitives to not only simplify control, but also improve performance. When allowed to exploit stable attractor behavior, humans may free up attention for accuracy demands.
the post location. The two dashed lines in Fig. 1C show ball trajectories that went through the target with zero error. Note that these two trajectories were released with two different arm angles and velocities. This exemplifies the redundancy of the task; zero error could be achieved with many different combinations of release angle and velocity. The solid line represents a trajectory that passed the target with a non-zero error, as further highlighted in the zoomed view in the inset.

In experiment 1, the angular position of the manipulandum of the first five subjects was recorded with an analog potentiometer (Vishay Spectrol, Shelton, CT). However, this potentiometer was not sufficiently sensitive in detecting the angle change when the velocity was low. Hence, the potentiometer was replaced with a digital encoder (BEI Sensors, Goleta, CA) to collect the remaining 10 subjects in experiment 1 and subsequently all 16 subjects in experiment 2.

In experiment 1, the diameter of the ball and the target were 5 cm, and the diameter of the post was 50 cm; in experiment 2, ball and target were 2.5 cm, and the post was 25 cm in diameter. These changes made the task of hitting the target easier. The error of each throw was defined as the shortest distance between the ball path and the center of the target (Fig. 1C, inset). When the error was less than a threshold, set to be 1.1 cm in experiment 1 and 1.8 cm in experiment 2, the color of the target changed from yellow to green to indicate a successful target hit.

The physical model that generated the ball trajectories consisted of the ball fixed to the center location by two orthogonal massless springs; the rest position of the ball defined the origin of the workspace coordinates, coincident with the location of the center of the post (Fig. 1C). The equations for the ball position in the x- and y-directions at time \( t \) were

\[
x(t) = A_x \sin(\omega t + \varphi_x) e^{-\frac{t}{\tau}} \\
y(t) = A_y \sin(\omega t + \varphi_y) e^{-\frac{t}{\tau}}
\]  

The frequency \( \omega \) denotes the natural frequency of the springs. The amplitudes \( A_x \) and \( A_y \), and the phases \( \varphi_x \) and \( \varphi_y \), of the springs were determined by the position and velocity of the ball at the moment of release. The exponential term with the time constant \( \tau \) created a small damping effect on the ball trajectory. Details of the physical model were presented in previous studies (Cohen and Sternad 2009; Hasson et al. 2016; Müller and Sternad 2004; Zhang et al. 2018).

**Experimental Design and Task Specifications**

Figure 2 overviews the specific experimental design, the virtual workspace, and the solution space for the two experiments. In experiment 1, 15 subjects performed 11 days of practice, with 240 throws parsed into 4 blocks of 60 throws with a brief rest between each block (2,640 throws in total). Each session lasted ~20 min (Fig. 2A). The subjects were instructed to hit the target (yellow) as accurately as possible and to avoid the center post (red). If the distance from the target was within the error threshold, the target color turned green to signal success. Importantly, they did not receive any cues about the temporal sequence of the throws, and they could wait between throws as long as they wanted or needed. The target was located at \((-60 \text{ cm}, 60 \text{ cm})\) referenced to the center post \((0 \text{ cm}, 0 \text{ cm})\); the natural frequency \( \omega \) of the springs was 3.16 rad/s, and the time constant \( \tau \) was 20 s. The pivot of the manipulandum was located at \((0 \text{ cm}, -150 \text{ cm})\), and length of the lever arm was 40 cm (Fig. 2B). The threshold for the error was 1.1 cm. After subjects released the ball, the elliptic trajectory was drawn on the screen for 1.4 s. During this time, the ball could not be grasped, and the initiation of a new throw had to wait for this minimum time.

An important property of the task is redundancy; a successful hit can be achieved with more than one ball release. As elaborated previously, both angular position and velocity determine the ball trajectory, and one value of error can be achieved by a mathematically infinite number of different combinations of angular position and velocity, defining a solution manifold (Müller and Sternad 2009; Sternad et al. 2014; Zhang et al. 2018). This feature of the task is illustrated in Fig. 2, C and F, in which angular position and velocity span the execution space and performance error defines the result space; different color shadings indicate the different levels of error. All solutions with zero error define a one-dimensional solution manifold. Although this feature was not used for the primary performance analysis, the solution manifold was important for the analysis of the Floquet multipliers (see below).

In experiment 2, 16 subjects were randomly assigned either to a self-paced group or to a discrete group. Both groups practiced the throwing task for 6 consecutive days with only 120 throws on each practice day, parsed into 4 blocks of 30 throws (720 throws in total, Fig. 2D). Subjects in the self-paced group received the same instruction as in experiment 1. Subjects in the discrete group were asked to position their arm in a rest zone at \(90 \pm 15 \text{ deg}\) after each throw; this rest zone was indicated on the screen by two white dashed lines (Fig. 2E). Subjects waited until they received a verbal

Fig. 1. Experimental task and set-up. A: real skittles game. B: virtual skittles game and how subjects interact with the virtual workspace. The subject stands in front of the backprojection screen, rests her arm on a manipulandum, and throws the ball around the red center post to hit the yellow target in the virtual workspace. C: top-down view with of post (red circle) and ball trajectories around the target (yellow). The ball trajectory describes an elliptic path around the post. The pink bars denote the rotating arm. 3 exemplary trajectories with the 2 dashed-line trajectories going through the target despite different release angle and velocities demonstrate the redundancy of the task. The solid line has a non-0 error, highlighted in the inset. The second inset shows a schematic of the 2D spring model for generating the trajectory of the virtual ball [see details of the model in Zhang et al. (2018)].
cue from the experimenter to start the next throw. This cue was timed by a computer to be 7 s after the initiation of the previous throw. As a throw lasted ~2 s, the instructed pause between successive throws was ~5 s. As the actual duration of each throw varied and the pause was relatively long, subjects did not perceive the interval as periodic.

The parameters of the task were modified to reduce the challenge and ensure relatively fast development of rhythmicity and also to test the generalization of the results from experiment 1. After pilot tests of different task conditions, the following parameters were chosen: target location (−30, 30 cm), ω = 3.14 rad/s, τ = 13.6 s, error threshold = 1.8 cm. The pivot of the manipulandum was also slightly shifted to the left and was located at (−10 cm, −65 cm) with a length of 30 cm. These modified parameters changed the result space and the solution manifold (Fig. 2).

Dependent Measures

Success rate and performance errors. A first measure of task performance was the success rate or percentage of successful trials per day, i.e., throws with errors below threshold. A related but finer-grained measure of performance was the error, defined by the minimum distance between the target and the ball trajectory (Fig. 1). The median error over all trials per day summarized each subject’s daily performance.

Periodicity of interthrow intervals. Periodicity is one essential characteristic of rhythmic movement, i.e., the same posture or event should recur at invariant intervals (Hogan and Sternad 2007). However, strict periodicity is unlikely to be present in human behavior, and in common understanding rhythmicity implies some variation around a constant interval. Figure 3 displays the time series of a self-paced trial of one subject on day 1 and on day 11. The red points mark the moments of ball release; the pink-shaded areas denote dwell times. Comparison of day 1 and day 11 clearly illustrates that the successive throws developed into an approximately periodic, i.e., rhythmic...
sequence. To quantify the degree of periodicity, the moments of ball release served as landmarks; the interval between two successive releases defined the interthrow interval (ITI). The median of all ITIs per day characterized each subject’s performance; ITIs longer than 10 s were removed, as they indicated a voluntary rest. The periodicity of movement was estimated by the dispersion of ITI, quantified by the quartile variation coefficient (QVC) of ITI for each day, as the distribution of ITI was highly leptokurtic and skewed (Bonett 2006).

\[
QVC = \frac{Q_3 - Q_1}{Q_3 + Q_1}
\]

where \(Q_1\) refers to the 25th percentile and \(Q_3\) to the 75th percentile of the distribution.

Number and duration of dwell times. Following definitions by Hogan and Sternad (2007), discrete movements were defined by dwell times between successive movements, whereas rhythmic movements do not have such pauses. Comparing day 1 with day 11 in Fig. 3A suggests that the dwell times indeed shortened or completely disappeared with practice. To quantify how the discrete throwing movements merged into a continuous sequence, the number and durations of dwell times between trials were quantified. Dwell time was defined as the interval between the termination of one throw to the initiation of the next throw (Fig. 3B).

For the identification of onset and offset of each throw, the angular position was smoothed with a Savitzky-Golay filter using a second-order polynomial model; the window length of the smoothing filter was set to 100 ms. Angular velocity was approximated by the slope of a linear fit to 20 smoothed-angle samples before the current time point; acceleration was calculated with the same method as for the velocity. The onset of a throw was indicated when the velocity surpassed 5 deg/s for 10 ms, and the acceleration continuously exceeded 50 deg/s² for 10 ms for the first time. The offset was identified when velocity returned to values smaller than 5 deg/s and acceleration remained smaller than 50 deg/s² for 10 ms. The time interval between an offset and onset of the next throw quantified the dwell time. If no clear initiation or termination was detected, the adjacent throws were considered part of continuous movements (Fig. 3A, bottom).

For all subjects, dwell times longer than 10 s were removed, indicating an explicit rest. This only happened six times in experiment 1 and never happened in experiment 2. The total number and the summed durations of dwell times per practice day served as two dependent measures for rhythmicity.

Variability and stability in state space. Previous work has highlighted that discrete and rhythmic movements have different flow topologies in state space (Huys et al. 2014; Schöner 1990; Sternad et al. 1998). We therefore plotted arm trajectories in state space, spanned by angular position and velocity, and examined their variability using Poincaré sections (Fig. 4). A Poincaré section is a discrete representation of the periodic flow of a continuous dynamical system, defined by the successive crossings of the Poincaré section. The topology of the Poincaré map and the Poincaré plot were previously examined to quantify the stability of human locomotion (Dingwell and Kang 2006; Hurmuzlu et al. 1994) and other physiological data, such as cardiac and respiratory signals (Glass and Mackey 1988; Honerkamp 1983; Winfree 1990).

Figure 4 shows exemplary orbits of the arm trajectories in state space (blue), together with the ball releases, denoted by black asterisks. Note that the state space is spanned by angle and velocity of the arm movements; when each state is viewed as a release of the ball trajectory, then each state also has an associated error. This is illustrated by the color shades as used previously in Fig. 2, C and F. The blue trajectories are intersected by a red line from the origin through the ball releases, the Poincaré section. The origin of the Poincaré section was determined for each subject and block separately as follows

\[
\text{center (angle,velocity)} = \frac{P_{2.5} (\text{angle,velocity}) + P_{97.5} (\text{angle,velocity})}{2}
\]

where \(P_{2.5}\) is the 2.5th percentile of the distribution of all angles and velocities, \(P_{97.5}\) represents the 97.5th percentile. The second point defining the section was the average location of release points in each day.
block, determined by the mean of the position and velocity values. Note that samples of the arm trajectory frequently did not lie exactly on the Poincaré section. Therefore, for each cycle of arm trajectory, the point closest to the Poincaré section ($\hat{d}_i$) was selected. The projections of all $\hat{d}_i$ onto the Poincaré section rendered the Poincaré map $d = [d_1, d_2, ..., d_n]$. Before the calculations of the Poincaré section and the Poincaré map, the state space was normalized. Therefore, the trajectories of all blocks of each subject were pooled, and the position and velocity axes were normalized by setting the average maximum and minimum of each variable to 1 and −1. The normalization was kept constant for each individual across all practice days when calculating the variability in Poincaré map and the Floquet multipliers. This allowed us to measure the changing variability across practice days. To maintain differences across subjects, each subject was normalized separately.

**Stability in state space.** To quantify the degree of stability of rhythmic movements, the Floquet multiplier has been widely used as a measure (Ahn and Hogan 2015; Hurmuzlu and Basdogan 1994; Kuo 1999). Human walking has been a primary application, and the moment of heel strike was chosen as the landmark for the Poincaré map. For the throwing movements, the cycle-by-cycle stability was characterized by the Floquet multiplier defined from the Poincaré map of the arm trajectories:

$$d_{i+1} - d_i^* = \lambda (d_i - d_i^*)$$

(5)

where $\lambda$ is the Floquet Multiplier, $d_i$ and $d_{i+1}$ represent the states at the $n$th and $(n+1)$-th cycle, and $d_i^*$ is the fixed point. A smaller Floquet multiplier value indicates faster convergence to the fixed point and therefore higher stability of the movement.

Previous studies on locomotion defined the fixed point $d_i^*$ as the average value of $d_i$, implying that different values of $d_i$ presented fluctuations around the mean that converged to the fixed point. However, in this study the mean value was not necessarily equivalent to the desired task performance and therefore did not represent the best estimate for the fixed point. A better choice was the point at which the performance error was zero. This value $d_i^*$ was given by the solution manifold and its intersection with the Poincaré map (Fig. 4A, inset). The Floquet multiplier was then defined by the eigenvalue of the one-dimensional map, determined by the slope of a simple linear regression of $d_{i+1}$ on $d_i$.

However, a recent study by Ahn and Hogan (2015) demonstrated that the estimation based on linear regression and related methods by Burg, Yule, and Walker (Burg 1967; Walker 1931; Yule 1927) resulted in systematic overestimations of $\lambda$ because of the limited length and the presence of noise in human behavioral data. Therefore, we applied their suggested correction method to obtain an unbiased estimate of the FM. This value $\hat{\lambda}$ was calculated as follows:

$$\hat{\lambda} = \hat{\lambda}_{YW} + \frac{\hat{\lambda}_{B_{\text{Burg}}} - \hat{\lambda}_{B_{\text{Burg}}}^{2n+1}}{(n - 1)(1 - \hat{\lambda}_{B_{\text{Burg}}}^2)}$$

(6)

where $\hat{\lambda}_{YW}$ represented the Yule-Walker equation and $\hat{\lambda}_{B_{\text{Burg}}}$ represented the Floquet multiplier calculated with Burg’s method based on spectral estimation.

**Statistical Analysis**

To characterize how performance and rhythmicity changed with practice in experiment 1, all eight dependent measures, median error, success rate, median ITI, VQC-ITI, total duration and total number of dwell times per block, mean STD-PM, and the FM of four blocks were subjected to one-way, repeated-measures ANOVAs with practice day as the within-subjects factor. Greenhouse-Geiser corrections were applied when the sphericity assumption was violated (Kirk 1982). Pairwise post hoc tests between practice days specified the change across days. To further assess whether rhythmicity in arm movements was associated with the performance error, Pearson’s correlation coefficients were computed between error and each of the dependent measures for each practice day.

In experiment 2, 2 (group) × 6 (practice days) repeated-measures ANOVAs were applied on the same dependent measures to determine whether discretizing movement influenced the performance. The same Pearson’s correlation coefficients were calculated for the discrete and the self-paced group.

**RESULTS**

**Experiment 1**

**Task performance: success rate and error.** Figure 5 shows that the success rate increased and the error decreased for all subjects across the 11 days of practice, as should be expected in this novel task. Individual subjects’ median values per day are represented by different colors, and the black points show the mean performance of the 15 subjects. The one-way ANOVA confirmed that the success rate significantly increased from $10.14 \pm 3.79\%$ to $23.28 \pm 5.90\%$, $F(5.50, 77.00) = 17.56, P < 0.001$, partial $\eta^2 = 0.56$ (Fig. 5A). Concomitantly, the errors significantly decreased from 6.90 cm ± 2.94 cm to 2.72 cm ± 0.80 cm, $F(1.88, 26.29) = 22.71, P < 0.001$, partial $\eta^2 = 0.62$ (Fig. 5C). With only very few exceptions, there was a continuous trend across all days, suggesting that improvement occurred throughout day 11.

To determine whether performance changed across days, pairwise $t$-tests compared the performance on each day with
the number of significant differences for each day with subsequent days. All metrics show significant changes over the 11 days of practice.

Comparing the actual number of significant pairings with this maximum number illustrates that both success rate and performance error decreased from day 1 to all other days at the beginning, with fewer significant changes in the middle but still some improvements at the final practice days. This performance improvement is to be expected but serves as the basis for further examination of rhythmicity and stability.

**Rhythmicity: periodicity of ITIs.** Both the ITI and its variability, QVC-ITI, decreased across practice days (Fig. 6, A and C). The ITI decreased from 2.38 ± 0.45 s to 1.90 ± 0.24 s, F(2.47, 34.55) = 12.42, P < 0.001, partial \( \eta^2 = 0.47 \). Although subjects became faster as practice progressed, their periodicity was not bounded by the minimum time between throws; this minimum time was the 1.4-s interval after ball release until it could be grasped again. Individual subjects varied in their ITI between 1.5 and 2.5 s. Pairwise comparisons between practice days suggested that subjects decreased the interval between throws predominantly during the first 4 days and then maintained their ITI on further days of practice (Fig. 6B).

The periodicity estimate QVC-ITI also decreased significantly from 0.10 ± 0.05 to 0.03 ± 0.01, F(2.13, 29.78) = 17.45, \( P < 0.001 \), partial \( \eta^2 = 0.56 \). Similar to ITI, QVC-ITI significantly dropped from day 1 to day 2, continued by a slow monotonic change until day 5 (Fig. 6D). These results support hypothesis 1, showing that subjects developed increasingly periodic arm movements. It is also noteworthy that the variability of ITI reached a level equivalent of 5%; this is very low, as even rhythmic movements synchronized with a metronome show similar variability.

**Correlation between periodicity and error.** For each day, the performance errors of all subjects were correlated with their respective ITI and QVC-ITI (Table 1). ITI appeared unrelated to error, and subjects who performed with shorter ITIs were not necessarily worse than those individuals with longer time between throws. Such relation might be conjectured if one assumed that error detection and correction would require time before each throw. In contrast, QVC-ITI showed significant correlations with mean error on early practice days (days 1–4). These results only weakly supported hypothesis 2.

**Rhythm: dwell time and number and duration of pauses.** The number and duration of pauses could only be calculated for the 10 subjects whose data were collected with the optical encoder (the potentiometer used for the first 5 subjects did not allow accurate detection of initiation and termination of movement). Figure 6, E and G, shows the number of pauses and dwell times across the 11 practice days. Overall, subjects inserted fewer pauses with practice, seen in the declining number of pauses per day from 163.90 ± 38.50 times to 86.70 ± 62.75 times, \( F(3.68, 33.11) = 4.75, P = 0.005 \), partial \( \eta^2 = 0.35 \). However, there was also a marked divergence in dwell times.

Table 1. **Pearson correlation coefficients** \( r \) between performance error and other dependent measures in experiment 1.

<table>
<thead>
<tr>
<th>Practice</th>
<th>ITI, s</th>
<th>QVC-ITI</th>
<th>Number of Pauses</th>
<th>Dwell Time, s</th>
</tr>
</thead>
<tbody>
<tr>
<td>Day 1</td>
<td>0.36</td>
<td>0.67</td>
<td>-0.16</td>
<td>0.30</td>
</tr>
<tr>
<td>Day 2</td>
<td>-0.10</td>
<td>0.42</td>
<td>-0.27</td>
<td>-0.23</td>
</tr>
<tr>
<td>Day 3</td>
<td>0.10</td>
<td>0.61</td>
<td>*0.01</td>
<td>0.09</td>
</tr>
<tr>
<td>Day 4</td>
<td>0.07</td>
<td>0.73</td>
<td>*0.18</td>
<td>0.35</td>
</tr>
<tr>
<td>Day 5</td>
<td>-0.28</td>
<td>0.48</td>
<td>-0.02</td>
<td>0.23</td>
</tr>
<tr>
<td>Day 6</td>
<td>-0.27</td>
<td>0.63</td>
<td>*-0.01</td>
<td>0.03</td>
</tr>
<tr>
<td>Day 7</td>
<td>0.15</td>
<td>0.41</td>
<td>0.20</td>
<td>0.06</td>
</tr>
<tr>
<td>Day 8</td>
<td>0.01</td>
<td>0.20</td>
<td>0.29</td>
<td>0.37</td>
</tr>
<tr>
<td>Day 9</td>
<td>-0.15</td>
<td>0.10</td>
<td>0.37</td>
<td>0.34</td>
</tr>
<tr>
<td>Day 10</td>
<td>-0.19</td>
<td>0.31</td>
<td>0.35</td>
<td>0.41</td>
</tr>
<tr>
<td>Day 11</td>
<td>-0.11</td>
<td>0.57</td>
<td>0.22</td>
<td>0.21</td>
</tr>
</tbody>
</table>

| ITI, interthrow interval; QVC-ITI, quartile variation coefficient of ITI. Sig., significance. *0.01 < \( P \) < 0.05, †0.001 < \( P \) < 0.01, ‡\( P \) < 0.001. The boldface numbers indicate the correlations that were significant.

**References:**

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Downloaded from www.physiology.org/journal/jn at Columbia Univ (129.236.163.087) on February 1, 2019.
between individuals; 4 subjects decreased at the beginning and retained only 15–50 pauses per day until the end, whereas the other 6 subjects fluctuated more across practice and retained between 100–200 pauses (the maximum number was 236 per day).

Unlike the pauses, however, most subjects significantly reduced their dwell times from a block total of 127.56 ± 71.70 s to 19.06 ± 23.93 s, F(2.03, 18.24) = 5.48, P = 0.013, partial η² = 0.38. Pairwise comparisons showed that both number of pauses and total dwell time dropped fast from day 1 to day 2 and then reached an asymptote after day 4 (Fig. 6, F and H). These changes are in support of hypothesis 1. However, counter to hypothesis 2, there was no significant correlation between performance error and number of pauses and dwell time (Table 1).

**Variability in state space: variability of Poincaré map.** The variability of the arm trajectory was quantified in state space, drawing a Poincaré section through the mean release points (Fig. 4). The standard deviations of the intersections at the Poincaré map were determined for each block, STD-PM, and then averaged across each day. As illustrated in Fig. 4B, the trajectories of the orbits across three exemplary days of a single subject became tighter and less variable. This observation was summarized in the average STD-PM of each day that significantly decreased from 45.94 ± 13.41 to 18.65 ± 6.12, F(3.12, 44.32) = 35.5, P < 0.001, partial η² = 0.72. Smaller STD-PM indicated that the hand trajectories occurred in every movement cycle with a similar state. This reduction in variability developed quickly over the first 3 days, then kept decreasing from day 4 to day 7 before it started to plateau on day 8 (Fig. 7B). This decrease was supportive of hypothesis 3.

**Stability in state space: Floquet multipliers.** The Floquet multipliers were calculated within each block and then averaged across the four blocks for each day. To begin, all Floquet multiplier values in the 10 subjects were <1, indicating that the rhythmic arm movements were dynamically stable (Fig. 7C). However, counter to hypothesis 3, movements within each subject did not become more stable as the changes of Floquet Multiplier across practice days were not significant, F(4.67, 65.34) = 2.05, P = 0.09, partial η² = 0.13. The individual subjects maintained similar Floquet multiplier levels or fluctuated across practice without any consistent trend. This was also reflected in the few significant pairwise comparisons (Fig. 7D).

However, the actual Floquet multiplier values differed significantly between the subjects. When we performed Pearson correlations between the performance error and the two stability metrics, strong positive correlations were revealed on all days (Table 1). Figure 8 visualizes these consistent results for both STD-PM and Floquet multiplier across all 11 days of practice. Figure 8, A and B, shows that subjects who had lower state space variability tended to perform better in the target-oriented throwing, as expected by hypothesis 3. The same strong positive correlations in Fig. 8, C and D, demonstrate that subjects who had smaller Floquet multiplier, i.e., higher stability, performed with lower errors.

**Experiment 2**

Two new groups of subjects performed the same skittles task but with a different target configuration and solution space that lowered the task difficulty. We expected that, with an easier task, rhythmicity should develop faster. Furthermore, if this task variation achieved comparable results, then this would also demonstrate some generality of the results in experiment 1.

**Task performance: success rate and error.** A first analysis of success rate and performance error clearly revealed that the self-paced group was better in the two metrics of task performance than the discrete group. As Fig. 9, A and B, illustrates, 6 days of practice with only 120 throws on each day was sufficient to show signs of approaching a plateau in success rate and performance error. The two-way ANOVA underscored that success rate significantly increased over days, F(3.11, 43.51) = 37.10, P < 0.001, partial η² = 0.73 (Fig. 9A), whereas the error significantly decreased in both groups, F(1.97, 27.62) = 27.83, P < 0.001, partial η² = 0.67 (Fig. 9B). More central to the hypothesis was that the subjects in the self-paced group showed a higher average success rate and lower errors than the discrete group. Although this group difference did not reach the level of significance for the success rate (P = 0.079), the advantage for the self-paced group was significant in the performance error, probably because error had a finer-grained resolution than the threshold-based binary success rate, F(1,14) = 4.86, P = 0.045, partial η² = 0.26. This result supported hypothesis 4.

One potential caveat is that there were no significant interactions (both measures P > 0.28) allowing for the possibility that the difference in performance might have been due to differences between the group’s general skill level. To probe whether this group difference was present at the very beginning of the experiment, we also compared the measures between the
self-paced and the discrete group on day 1 using two-sample independent t-tests. Neither success rate nor performance error were significantly different ($P > 0.05$); the differences only became significant on days 4 and 5. This subtle divergence did not reach significance in the interaction of the ANOVA. However, these results indicate that it was not differences in skill level between the two groups that brought about the overall better performance of the self-paced group. Rather, it was the disruption of the flow of successive throws that impacted performance.

**Periodicity: ITIs.** Measures of periodicity were only applicable for the self-paced group. Table 2 summarizes mean values of ITI and QVC-ITI over six practice days. Although a small visible decrease in both ITI and QVC-ITI was discernible, these changes did not reach significance in a one-way ANOVA. Because the target location in experiment 2 was less difficult to hit, subjects fell into a rhythm very early in practice and maintained the same regularity until the end of the much shorter practice. This is reflected in the very low QVC-ITI that reached 5% very early in practice. In fact, both ITI and QVC-ITI reached the same level as in experiment 1 on day 3. Hence, despite little change across practice days, the rhythmicity measures still replicated those of experiment 1 and were consistent with hypothesis 1.

**Rhythmicity: number and duration of dwell times.** As for periodicity, the measures for rhythmicity, i.e., number and duration of dwell times, could only be determined for the self-paced group. The one-way ANOVA showed no consistent changes in the number and duration of dwell times over the 6 days; 2 subjects decreased their number of pauses, whereas 3 decreased their dwell times among all 8 subjects. Comparing the mean values in Table 2, it becomes evident that the initial values were already very low and close to the values at the end of experiment 1. Hence, these low levels allowed for very little change.

### Table 2. Measures of rhythmicity in experiment 2

<table>
<thead>
<tr>
<th>Practice Day</th>
<th>ITI, s</th>
<th>QVC-ITI</th>
<th>Dwell Time, s</th>
<th>Number of Pauses</th>
</tr>
</thead>
<tbody>
<tr>
<td>Day 1</td>
<td>2.45 ± 0.48</td>
<td>0.07 ± 0.02</td>
<td>71.70 ± 64.76</td>
<td>87.38 ± 26.23</td>
</tr>
<tr>
<td>Day 2</td>
<td>2.42 ± 0.52</td>
<td>0.05 ± 0.05</td>
<td>72.13 ± 64.38</td>
<td>81.25 ± 35.17</td>
</tr>
<tr>
<td>Day 3</td>
<td>2.31 ± 0.34</td>
<td>0.05 ± 0.02</td>
<td>56.82 ± 43.22</td>
<td>83.75 ± 34.95</td>
</tr>
<tr>
<td>Day 4</td>
<td>2.16 ± 0.24</td>
<td>0.05 ± 0.01</td>
<td>40.72 ± 33.74</td>
<td>79.00 ± 36.70</td>
</tr>
<tr>
<td>Day 5</td>
<td>2.17 ± 0.27</td>
<td>0.04 ± 0.01</td>
<td>48.30 ± 40.70</td>
<td>85.63 ± 34.37</td>
</tr>
<tr>
<td>Day 6</td>
<td>2.11 ± 0.23</td>
<td>0.04 ± 0.01</td>
<td>38.59 ± 33.70</td>
<td>83.50 ± 36.09</td>
</tr>
</tbody>
</table>

Values are means ± SE. ITI, interthrow interval; QVC-ITI, quartile variation coefficient of ITI.
Stability in state space. As summarized in Fig. 10F, the Floquet multiplier values of both groups were between 0 and 0.4, with the exception of one extreme outlier in the discrete group. Note that this subject was not an outlier in the other performance measures, suggesting that subjects could indeed perform with the entire range of Floquet multipliers. As in experiment 1, there were no significant effects across practice days (P = 0.07) nor between the two groups (P = 0.08). Pearson correlations between the performance error and the two stability measures were summarized in Table 3. As can be seen, STD-PM in the discrete group correlated significantly with error in 5 out of 6 days, consistent with hypothesis 3. The lack of correlation may be ascribed to the fewer subjects that displayed a smaller range of Floquet multiplier values than in experiment 1.

DISCUSSION

The findings of the two experiments conclusively demonstrate that subjects spontaneously developed a stable rhythm when performing a sequence of similar movements. Rhythmicity was defined by metrics that quantified the degree of periodicity and continuity. Stability was evaluated in state space using the Poincaré map. Experiment 1 documented how subjects spontaneously developed rhythmicity over extensive practice; variability of ITIs decreased, and pauses between throws became fewer and shorter (hypothesis 1). Subjects with higher degrees of rhythmicity and stability of their arm trajectory also achieved better task performance (hypothesis 2). Although variability at the Poincaré section noticeably decreased, stability as quantified by the Floquet multipliers did not change with practice (counter hypothesis 3). Nonetheless, subjects that exhibited smaller Floquet multiplier values, indicating higher stability, performed with smaller errors. Experiment 2 explicitly disrupted periodicity and continuity, which had a negative effect on errors and success rate, as predicted by hypothesis 4.

At first glance, the observation that subjects fall into rhythm may appear almost trivial, as it concurs with intuitive experiences and anecdotal observations. However, it needs to be reiterated that in the throwing movements, the explicit and only goal of the subjects was to minimize their error when aiming to hit a target. The intervals between successive ball releases became increasingly invariant, without explicit awareness of this development. The variability of the ITIs in both the 11-day-long but also in the shorter practice dropped to levels as low as observed in the highly practiced thrower of experiment 2.

Table 3. Pearson correlation coefficients \( r \) between error and dependent measures in experiment 2

| Practice Day | Self-Paced Group | | Discrete Group | |
|--------------|------------------|------------------|------------------|
|               | STD-PM | FM | STD-PM | FM |
| Day 1        | 0.61   | 0.38 | **0.76** | 0.16 |
| Day 2        | 0.24   | -0.22 | 0.53 | 0.71 |
| Day 3        | 0.49   | -0.27 | **0.87** | †**0.79** |
| Day 4        | 0.60   | -0.27 | 0.76  | *-0.21 |
| Day 5        | 0.75   | *-0.27 | **0.93** | †0.57 |
| Day 6        | 0.65   | -0.34 | **0.91** | †0.21 |

Sig., significance. *0.01 < P < 0.05; †0.001 < P < 0.01. The boldface numbers indicate statistically significant correlations.
One plausible explanation for the emerging rhythmicity could be that subjects get attracted to the resonant frequency of the oscillating limb, which may confer an energetically parsimonious solution as smaller input forces generate higher amplitude output. Such an argument has been supported by a number of studies in locomotion in which the human or animal tends to prefer a frequency that coincides with the minimum of metabolic energy consumption (Hoyt and Taylor 1981; Snaterse et al. 2011). Other work demonstrated that the preferred frequencies scale proportional to the resonant frequency of the limb (Holt et al. 1990, 1995; Turvey et al. 1988). For the human arm moving in the horizontal plane (as in skittles), several studies have assessed stiffness and damping (Bennett 1993; Bennett et al. 1992; Latash 1992), but the resonant frequency itself has been given less attention. With the use of perturbation methods, these studies quantified the stiffness of the neuromuscular complex and its variations throughout the cycle. However, not only do these stiffness estimates vary across the cycle, different studies also identified widely different stiffness values, ranging between 2 and 18 N-m/rad (Bennett et al. 1992) and 6 to 22 N-m/rad (Latash 1992). This is probably due to different choices of movement frequencies and specified movement amplitudes. Another set of studies examined rhythmic movements in the sagittal plane, in which the pendular movements are also subject to restoring torques attributable to gravity, absent in movements in the horizontal plane in which stiffness alone is the determinant (Bingham et al. 1991). For forearm movements swinging in the sagittal plane, Hatsopoulos and Warren (1996) estimated the resonant frequency to be around 1.2 Hz and the joint stiffness to be 0.4 N-m/rad. This study demonstrated that subjects indeed exploited the resonant frequency when allowed to swing their limb at their preferred frequency.

To assess whether the limb movements in the skittles task converged to their respective resonant frequencies with potential energy savings, it would be necessary to know not only the inertial parameters of the limb and the manipulandum, but also the values for the muscle stiffness and damping. Moreover, as visible in the phase portrait in Fig. 4, the throwing task goes beyond simple forearm oscillations and includes accentuated hand opening for the ball release. Furthermore, the effective resonant frequency should probably not only be defined for the moving forearm plus hand, but also include the ball trajectory, as its dynamics is coupled to the hand. Quantifying this “resonant frequency” over the entire perception-action cycle is clearly a challenge. To conclude, although it is possible or even plausible that the emerging ITI converges to a period that affords low metabolic cost or effort, this is hard to quantitatively support at this point.

One benefit of rhythmic performance with dynamic stability is its robustness with respect to perturbations and noise (Longtin et al. 1990; Stark 1962). By definition, any system with stable limit-cycle dynamics rejects small errors and noise and returns to its stable attractor without requiring explicit corrections. Empirical support that this feature of dynamic systems is relevant for human motor behavior has been provided in a series of studies on rhythmically bouncing a ball to a target height (de Rugy and Sternad 2003; Huber and Sternad 2015; Sternad et al. 2000, 2001a, 2001b). Although the racket can contact the ball at any phase of the racket movement and achieve the desired target amplitude, mathematical analyses showed that only contacts at the decelerating portion of the racket trajectory show dynamic stability. Subjects indeed converged to this phase of contact with practice, without being explicitly aware of it. These studies argued that exploiting dynamic stability is a computationally parsimonious solution,
obviating computationally demanding error correction (Schaal et al. 1996; Sternad 2017; Wei et al. 2007). However, in contrast to the throwing movements, bouncing a ball in the air is a rhythmic activity, and subjects were instructed to rhythmically bounce the ball. When performing a sequence of throws, periodic movements were not required.

From a neurophysiological perspective, rhythmic movements may confer an advantage because they may involve fewer high-level neural resources. Using fMRI imaging, Schaal, Sternad, and colleagues (Schaal et al. 2004) demonstrated that rhythmic wrist movements required significantly fewer cortical and subcortical areas than discrete movements that were voluntarily separated by random pauses. Discrete movements were associated with bilateral parietal and cerebellar activation, not seen in self-paced rhythmic movements. Presumably, control of rhythmic movements is deferred to subcortical and possibly brainstem areas although these brain regions were not recorded. This view is also supported by a study on patients with stroke that revealed less impairment in rhythmic movements compared with discrete movements in patients with cortical stroke (Leconte et al. 2016). If rhythmic movements can be maintained with fewer demands on higher-level cortical control, then they may free up computational capacity for other control processes.

This preference for stable rhythmic actions is also good support for the proposition in motor control that movements are generated by dynamic primitives. Previous work has argued that the control of the complex human system requires modules to simplify control of the high-dimensional and redundant system. Several lines of research have pursued such modules in the muscular organization and identified functional low-dimensional synergies (d’Avella et al. 2003, 2006; Ivanenko et al. 2004; Tresch et al. 1999). For example, several studies examined locomotion in humans and identified four or five synergies in muscle activation in control of the movement (Dominici et al. 2011; Ivanenko et al. 2004, 2005). Examining walking on a narrow beam, dancers exhibited better control of balance, which was associated with additional synergies (Sawers et al. 2015).

In contrast to muscle synergies, a dynamic systems perspective proposes that modules or primitives are defined over the neuromuscular substrate within the context of a behavioral task. Sternad and colleagues (Schaal and Sternad 1998; Schaal et al. 2000; Sternad 2008; Sternad et al. 2000) have proposed stable attractors as modules that are assembled over the neuromechanical system. Recognizing that the neuromechanical system is nonlinear, stable attractors can take the form of fixed points and limit-cycles, generating discrete and rhythmic movements, respectively. Such stable subsystems may combine to perform more complex movements as a combination of both (de Rugy and Sternad 2003; Ronsse et al. 2009; Sternad et al. 2000). More recently, Hogan and Sternad (2012, 2013) proposed that a third primitive, impedance, is needed to ensure stable physical interactions with objects and the environment. They outline a nonlinear equivalent network as a model for integrating the primitives into interactive behavior.

Although the observations have been recorded in the ideal conditions of the laboratory, the phenomenon is likely to be upheld in more realistic conditions with environmental disturbances, just as the rhythmicity of walking and running is maintained on uneven terrain. How robust this tendency is requires further investigation. It is noteworthy though that this preference for rhythmic movements is also consistent with several clinical observations. For example, individuals with severe autism frequently are urged to perform repetitive movements, such as hand flapping and body rocking, that seem to have a calming effect (Bodfish et al. 2000; Goldman et al. 2009). Individuals with chronic schizophrenia frequently display purposeless repetitive movements, and antipsychotic drugs can induce low-frequency large-amplitude tremor (Burke et al. 1982). Furthermore, it is well known that one cardinal symptom of Parkinson disease is tremor with higher-amplitude and lower frequency compared with healthy physiological tremor (Heldman et al. 2011). A similar manifestation of uncontrolled oscillations is essential tremor, another widespread but still understudied neurological disorder (Archert et al. 2018a, 2018b; Elble 2017). These pathological manifestations suggest that, when the nervous system is impaired, oscillations as a more basic form of organization can emerge.

As a final speculation, we want to return to the recognition that the human system is a complex hierarchy of interconnected oscillations at different temporal and spatial scales. As many scientists in chronobiology have pointed out, the human body comprises a hierarchy of oscillatory processes at a vast range of orders of magnitudes, starting with periods 10−3 and 10−1 s at the level of neuronal signals, to 100–102 s at the level of cardiac and respiratory processes, to the level of the metabolic system with 103 to 105 s and even higher in circadian and reproduction cycles. The behavioral level of volitional movements is at the order of 104 s. However, the intriguing fact is that movements are under volitional control and can take on many complex nonrhythmic patterns. The observation that a sequence of volitional movements tend to shape into a rhythmic pattern suggests that it falls in line with the hierarchical system whenever possible.

Returning to the subjective association of rhythmic movements with “being in a zone,” signaling a comfortable state, this may suggest that rhythmic behaviors have beneficial effects on the human system, just as rocking has soothing effects on an infant (Ko et al. 2016). We conclude by proposing that the central nervous system can make use of this intrinsic tendency and exploit such temporary rhythmic patterns as building blocks or primitives to construct more complex movement patterns. We recognize that much of these interpretations are still highly speculative and call for more research in this direction.